## Student Activity: To investigate the addition of complex numbers

Use in connection with the interactive files, 'Addition of complex numbers', and 'Addition by translation of a complex number', on the Student's CD.


1. Add the following complex numbers and check your answers using the interactive file "Addition of Complex numbers".

|  |  | Calculate $z_{1}+z_{2}$ |
| ---: | :--- | :--- |
| a. | $z_{1}=3+2 i$ and $z_{2}=1+4 i$ |  |
| b. | $z_{1}=2+3 i$ and $z_{2}=1+3 i$ |  |
| c. | $z_{1}=2+4 i$ and $z_{2}=1-3 i$ |  |
| d. | $z_{1}=2+4 i$ and $z_{2}=-1-2 i$ |  |
| e. | $z_{1}=-3+4 i$ and $z_{2}=1-2 i$ |  |
| f. | $z_{1}=-2-4 i$ and $z_{2}=1-3 i$ |  |
| g. | $z_{1}=-1-3 i$ and $z_{2}=-2-1 i$ |  |
| h. | $z_{1}=i$ and $z_{2}=2+i$ |  |


| i. | $z_{1}=i$ and $z_{2}=i$ |  |
| ---: | :--- | :--- |
| j. | $z_{1}=i$ and $z_{2}=-i$ |  |
| k. | $z_{1}=1$ and $z_{2}=-1$ |  |
| I. | $z_{1}=1$ and $z_{2}=-i$ |  |
| m. | $z_{1}=-1-i$ and $z_{2}=-2-i$ |  |
| n. | $z_{1}=-1-i$ and $z_{2}=-2-i$ |  |
| o. | $z_{1}=1+i, z_{2}=-2-2 i$ and $z_{3}=2+3$ |  |
| p. |  |  |

2. What shape is formed when you add two complex numbers?
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3. What complex number would you need to add to $2+3 i$ to get $0+0 i$ ?
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4. If two complex numbers $z_{1}$ and $z_{2}$ are added together to give $4+6 i$, list four values $z_{1}$ and $z_{2}$ could have.
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$\qquad$
5. Is the addition of complex numbers associative? Explain your answer.
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a. Plot the following complex numbers in the Argand Diagram.
i. $2+4 i$
ii. $2-2 i$
iii. $-3+i$
iv. $-2-3 i$

b. Add $2+1 i$ to each of the complex numbers in section a. of this question (It is not necessary to show the parallelograms).
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$\qquad$
$\qquad$
c. Draw a directed line (a line with an arrow indicating direction) between each complex number and its corresponding number with $2+1 i$ added to it. What do you notice?
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$\qquad$
d. What would have happened if instead of adding the complex number $2+1 i$ to each of the complex numbers above you had subtracted $2+1 i$ ?
