

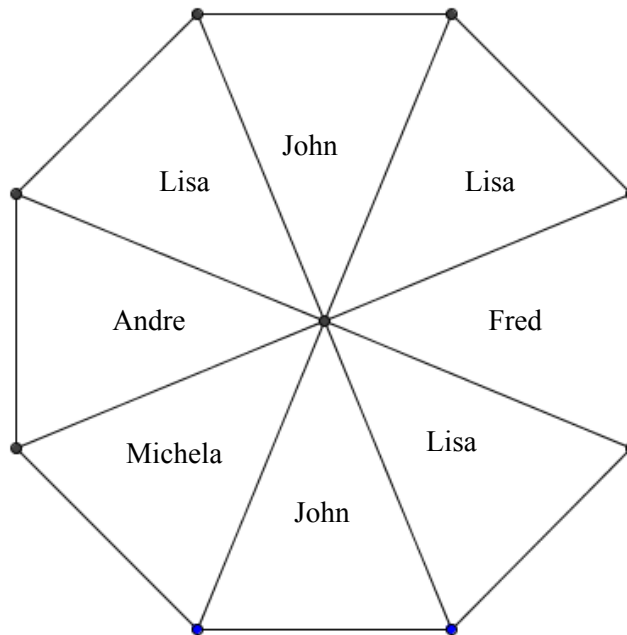
Foundation level Maths

(Probability and Statistics)

Sample Questions

Question 1

The spinner below is a regular octagon. It can land on any name.



- Which name is the spinner most likely to land on?
- Which two names is the spinner equally likely to land on?
- Write down a name, which the spinner **cannot** land on.
- Is the spinner more likely to land on a boy's or girl's name?
- The spinner is spun 200 times. How many times would you expect it to land on the name Lisa?

Suggested Solution

- Lisa. There are three sections with her name on it.
- Three names are equally likely to land on. Fred, Michela and Andre
- Mary or any name that is not Lisa, Fred, John, Michela or Andre.
- Depends who is a girl. Assuming Michela is a girl and Andre is a boy, they are equally likely.
- $200(3/8) = 75$

Question 2

Choose from

Impossible	Certain	Likely	Unlikely	Evens
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to describe the probability of each of the following.

- (a) An ordinary coin when tossed will show “heads”.
- (b) Everyone in a class at school will have the same colour of hair.
- (c) You will pick a black ball out of a bag only containing black balls.
- (d) An ordinary die will land on an 8.

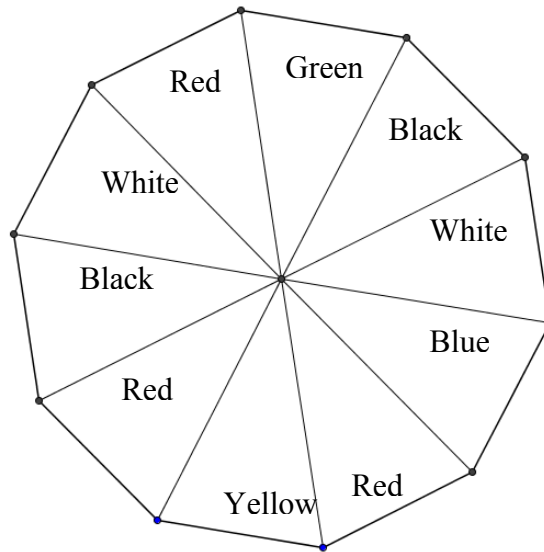
Suggested Solution

- (a) Evens
- (b) Unlikely
- (c) Certain
- (d) Impossible.

Question 3

For the spinner shown find:

- (a) Which colour is the spinner most likely to land on?
- (b) Least likely to land on?
- (c) How many more times likely is Black than Yellow?
- (d) Redesign the spinner so that Black is four times more likely than yellow.



Suggested Solution

- (a) Red
- (b) Blue, green or yellow all have equally probability.
- (c) Twice
- (d) 4 black and 1 yellow

Question 4

A bag contains 19 balls, 7 are red, 8 Green and 4 White.

One disc is selected at random.

- (a) Are all outcomes equally likely? Explain your reasoning.
- (b) Calculate, the probability that it Red.
- (c) How many Green balls would you have to add so that the probability of picking white is 0.16.

Suggested Solution

- (a) No a green ball is more likely as 8 out of 19 balls are green and only 7 out 19 are red and 4 out 19 are white.
- (b) $\frac{7}{19}$
- (c) $0.16 = \frac{4}{x} \Rightarrow x = 25$, in total. Assuming the number of red and white stay the same we would need 14 green in all so we would need to add 6 green balls.

Question 5

A fair coin is tossed and a die is thrown. Make out a sample space for this experiment and find the probability of getting a tail on the coin and an odd number on the die.

Suggested Solution

H1	T1
H2	T2
H3	T3
H4	T4
H5	T5
H6	T6

$$\frac{3}{12} = \frac{1}{4}$$

Question 6

The table below shows some of the probabilities of selecting a coloured ball in one draw from a bag containing balls of four different colours..

Colour	Red	Blue	Green	Black
Probability	0.3	0.4	0.1	

Calculate the probability of getting

- (a) A Black ball
- (b) A Green or Blue ball

Draw a sketch of a spinner with four colours that would give that would also give these probabilities.

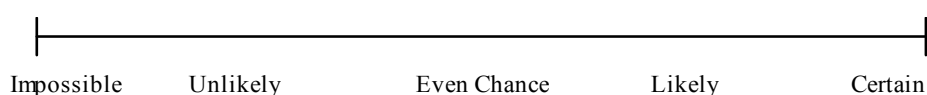
Suggested Solution

- (a) 0.2
- (b) 0.5

Divide into 10 equal sections - 3 red sections, 4 blue sections 1 green section and two black sections

Question 7

Use the probability line below to choose the best words to describe the probability of each of the named events taking place.



Choosing a random day of the week

Ending in Y

Beginning with W

Beginning with a T or and S

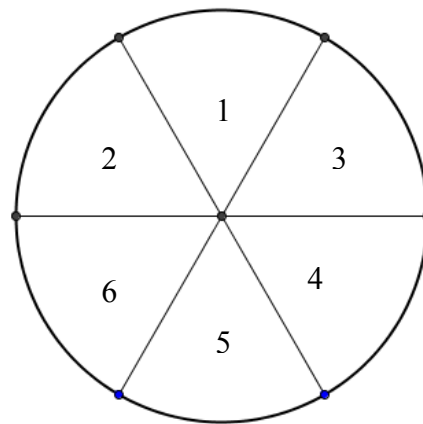
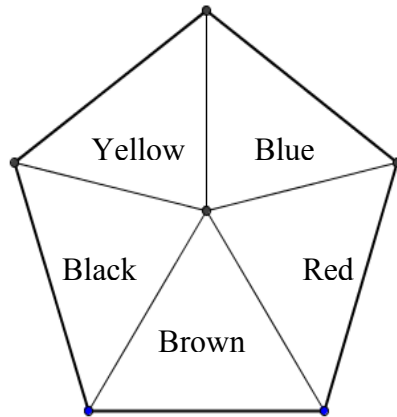
Having less than six letters

Suggested Solution

- (a) Certain
- (b) Unlikely
- (c) Likely
- (d) Impossible

Question 8

The diagrams below represent two spinners. Make out the sample space for the outcome when both spinners are spun.



- Find the probability of a red on the first spinner and a 4 on the second
- Find the probability of a colour beginning with the letter B and an even number
- Redraw the second spinner so that an even number is twice as likely as an odd number.

Suggested Solution

Yellow, 1	Red, 1	Blue, 1	Brown, 1	Black, 1
Yellow, 2	Red, 2	Blue, 2	Brown, 2	Black, 2
Yellow, 3	Red, 3	Blue, 3	Brown, 3	Black, 3
Yellow, 4	Red, 4	Blue, 4	Brown, 4	Black, 4
Yellow, 5	Red, 5	Blue, 5	Brown, 5	Black, 5
Yellow, 6	Red, 6	Blue, 6	Brown, 6	Black, 6

(a) $\frac{1}{30}$

(b) $\frac{9}{30} = \frac{3}{10}$

(c) 9 sections with two each for 2, 4 and 6 and one section for 1, 3 and 5.

Question 9

The table shows some information about the residents of Gauss Avenue.

	Walk to work	Cycle to Work	Total
Car Owners			
Bicycle Owners		22	35
Total	40		100

- (a) Fill in the missing numbers in the table
- (b) What is the probability that a resident chosen at random will:
1. Walk to work”
 2. Owns a bicycle and cycles to work?
 3. Owns a car and walks to work?

Suggested Solution

	Walk to work	Cycle to Work	Total
Car Owners	27	38	65
Bicycle Owners	13	22	35
Total	40	60	100

1. 0.4 2. 0.22 3. 0.27

Question 10

John and Martin counted the counted the number of car number plates contained the letter P. They recorded their results as shown below.

John		Martin	
Number of Cars with P	Number without P	Number of Cars with P	Number without P
80	20	237	63

- (a) Whose set of results gives the best estimate of the probability of a car number plate containing the letter P? Explain your reasoning.
- (b) If Martin were to count 600 cars in total, approximately how many would he expect to contain the letter P on their plates?

Suggested Solution

- (a) Martin- his sample is bigger. (b) $\frac{237}{300} \times 600 = 474$

Question 11

500 tickets numbered 1 to 500 are sold for a raffle.

What is the probability that the winning ticket has a number greater than 350?

Explain why the probability that a male has the winning ticket may not be $\frac{1}{2}$.

Suggested Solution

$$\frac{150}{500} = \frac{3}{10}$$

We are not told how many males bought tickets.

Statistics**Question 12**

The data shows the number of minutes spent reading by twenty-five children each evening after schools.

18 21 35 15 19 14 29 25 22 31 3 5 42
7 11 28 14 18 26 32 16 8 12 14 15

- (a) Use the data to make a stem and leaf diagram
- (b) Write down the modal number of minutes spent reading
- (c) What is the median number of minutes spent reading?
- (d) How many children spent more than more than 29 minutes reading each evening?

Suggested Solution

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0 | 3 5 7 8
1 | 1 2 4 4 4 5 5 6 8 8 9
2 | 1 2 5 6 8 9
3 | 1 2 5
4 | 2
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Key : 3|1 means 31

- (b) 14
- (c) 18
- (d) 4

Question 13

Seven of the students in Class 2A do a morning paper round. The numbers of papers delivered by the students each Monday are:

21,18,24,26,14,31,26

- (a) What is the range of the number of papers delivered?
- (b) What is the mean number of papers delivered?
- (c) John is starting his paper round next week how many papers should he deliver if the mean number of papers delivered is to increase.

Suggested Solution

- (a) $14-31=17$
- (b) 22.86
- (c) 23 or more

Question 14

The diagram below shows the number of DVDs owned by twenty university students.

Key: 15|3=18 Note: Unusual Key. $15 + 3 = 18$

0						
5	2	4				
10	1	2	2	4		
15	2	2	2	3	4	
20	1	2	2			
25	0	1	3			
30	0	1	1			

- (a) How many students own between 15 and 20 DVDs?
- (b) What is the difference between the greatest number of DVDs owned and the fewest? What is the mode of this data set?
- (c) What other type of chart could be used to represent this data?

Suggested Solution

- (a) 5
- (b) Between 7 and 31 so difference is 24
- (c) 17
- (d) Dot plot

Question 15

Julie is a pupil at Presentation Secondary School, Ballymac. It is an all-girls school. She wishes to know how many times a month, on average, the people in Ballymac go to the swimming pool. She asks 500 pupils in her school.

Give **two** reasons why Julie's sample may not be representative of the people in her town.

Suggested Solution

Sample are all school going age and are all girls so will not represent the town's population.

Question 16

The number of books in the bags of students in first year was recorded.

(a) How many pupils are in first year?

(b) Which is the most common number of books per bag?

Why do you think this is so?

(c) If the survey were carried out

in fifth year would you expect that same result? Draw a suitable chart to represent the data.

Number of Books	Number of Bags
5	4
6	6
7	6
8	10
9	12
10	6
11	4
12	2

Suggested Solution

(a) 50

(b) because 12 people have 9 books and this is the largest number of people in any of the categories

(c) No as 5th years may have more books. Bar-chart or dot plot

Question 17

Forty pupils were asked to write down an odd number less than 10, the results are shown below.

1 5 9 3 1 7 9 5 5 5
3 3 9 7 7 7 5 1 3 7
9 5 1 1 3 7 9 5 3 9
3 3 7 7 1 1 9 3 5 7

(a) Complete the following frequency distribution table.

Odd Number	Frequency
1	
3	
5	
7	
9	

(b) Draw a clearly labelled bar chart to represent the data

Suggested Solution

Odd Number	Frequency
1	7
3	9
5	8
7	9
9	7

Question 18

The data below represents the times for eleven students in an egg-and-spoon race at a school's sports day. Discuss the best ways of representing this type of data.

Names	Times (seconds)
Anthony	25
Emma	18
Shane	27
Leona	22
Paul	20
Molly	25
Henry	17
Tanya	23
Thomas	23
Maria	26

Suggested Solution

Bar-chart as you can see clearly each student's times

Question 19

The data below describes the wind during the month of January.

Discuss the best ways of representing this type of data.

Wind Type	Days
Strong Wind	10
Calm	5
Gale Force	7
Light Breeze	9
Total	31

Suggested Solution

A pie chart, as all the days in the month were recorded. You could also use a bar chart.

Question 20

Below is a recipe for a cake. . Discuss the best ways of representing this type of data.

Ingredients	Measurements
Margarine	6 oz
Self-Raising-Flower	1 lb
Caster Sugar	6 oz
Sultanas	2 oz
Vanilla Essence	0.25 tsp
Eggs	3

Suggested Solution

Difficult to represent this data in any chart as eggs have no given weight and neither has vanilla essence.

Question 21

James is designing a questionnaire to test the idea that “the amount of sleep you need changes with age”.

One of his questions will find out the ages of those being questioned.

- (a) Write a suitable question he could ask, with response boxes for people to tick.
- (b) Having completed his questionnaire James decided to give it out to all his school friends and their parents. Give one reason why this is not a good sample.

Suggested Solution

- (a) What is the average number average number of hours you sleep per night? (Answer in whole numbers). Please tick one the boxes below:

Note 10-20 means 10 and less than 20 etc.

Age	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80	Over 80

- (b) Children and parents are not a representative sample of all the age groups in the population.

Question 22

The times taken by a group of men to complete a questionnaire are shown in the table below

Times (Minutes)	Frequency
0 – 5	36
5 – 10	35
10 – 15	25
15 – 20	15
20 – 25	10
25 – 30	8

- (a) How many men completed the questionnaire?
- (b) Draw a clearly labelled histogram to represent this data.
- (c) If a person was chosen at random, what is the probability that he completed the questionnaire in less than 15 minutes?

Suggested Solution

(a) 129

(c) $\frac{96}{129} = \frac{32}{43}$

Question 23

School reports for students sometimes show the student's mark and the average mark for the year group. Which of the three measures of "average" do you think they should use? Give a reason for your answer.

Suggested Solution

Mean because all the marks contribute to the mean. If the majority of the class got high marks the average would be high and if the majority of the class got low marks the mean would be low. However the mean would be affected by outliers. The median would be a better representation if there are outliers as it is unaffected by outliers.

