

# Purpose

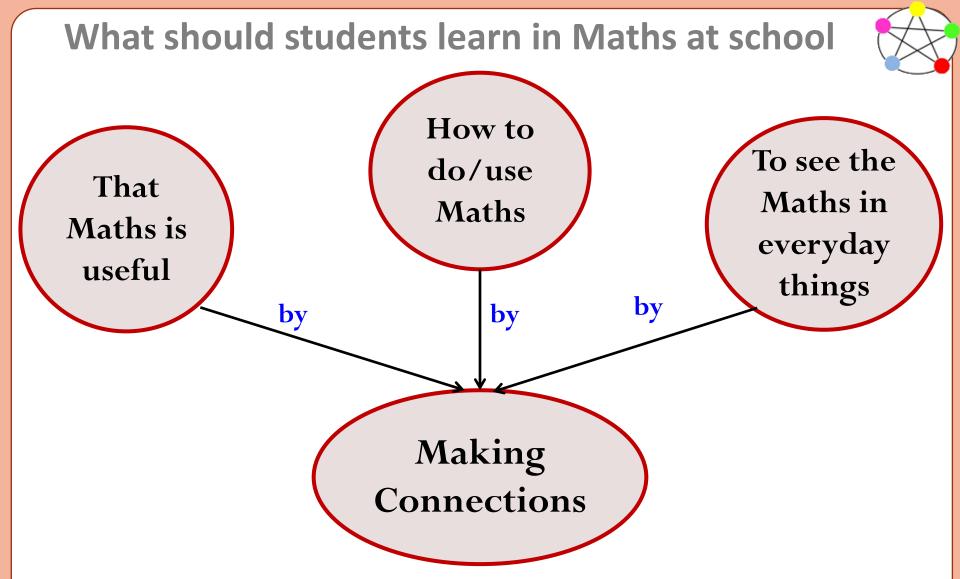


The purpose of this section is:

To identify the importance for Teaching & Learning of making connections

To consider the types of connections it is beneficial to make

To alert us as a community of educators to the importance of connecting with the school literacy and numeracy policy.



"It is essential to make connections in mathematics if one intends to develop mathematical understanding."

#### Mathematical understanding involves ...

Strategic

Comnete

Productive

Disposition

Procedural





- knowing-how (doing)
- knowing-*why* (explaining)
- knowing-*when* (applying)

Among the objectives of Junior Certificate Mathematics are to develop

•• procedural fluency—skill in carrying out procedures flexibly, accurately, efficiently, and appropriately

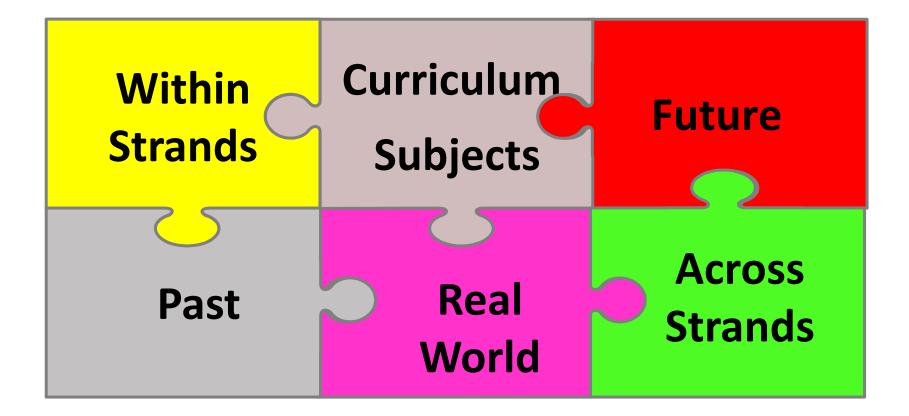
•• adaptive reasoning—capacity for logical thought, reflection, explanation, justification and communication

•• strategic competence—ability to formulate, represent, and solve mathematical problems in both familiar and unfamiliar contexts



# To Make Connections in Mathematics

# What does this mean for you?





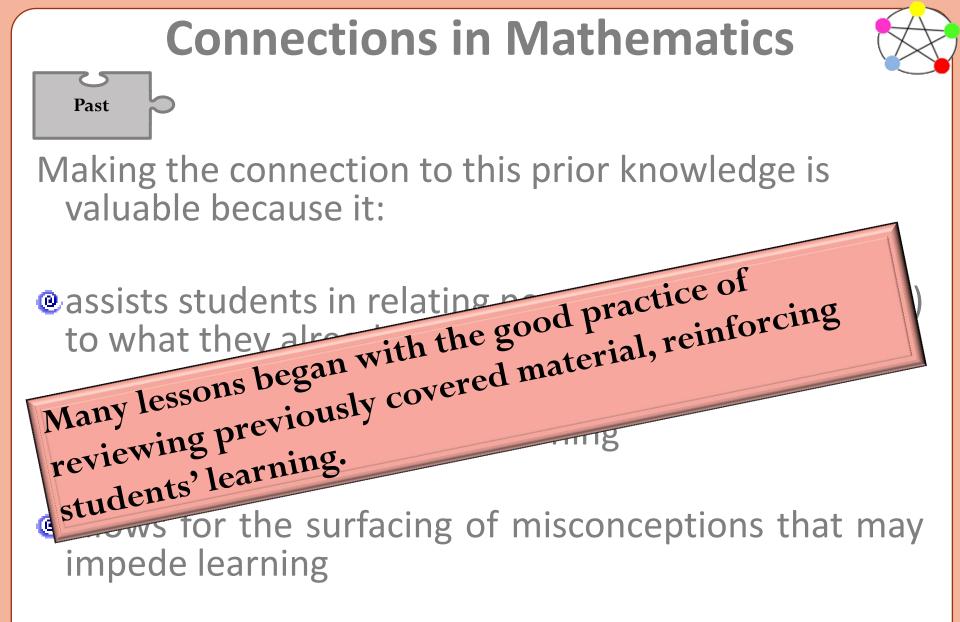
Making connections is an important human activity.

Past

"Seeking patterns and connections is the natural activity of the brain."

Caine &Caine 1990

Isolated pieces of information require more time to assimilate than learning experiences that are connected with a person's prior knowledge.



eidentifies gaps in knowledge or skills that may exist

Past



### The History of Mathematics

"No subject loses more when divorced from its history than mathematics"

Bell E.T



The History of Mathematics

eHumanises Mathematics

Students' problems have been present in history

Cultural links

Past

Foundation for better understanding

e Highlights interaction between mathematics & society





Without an explicit focus on connections, students may view their learning of mathematics as the accumulation of unrelated and discrete ideas.

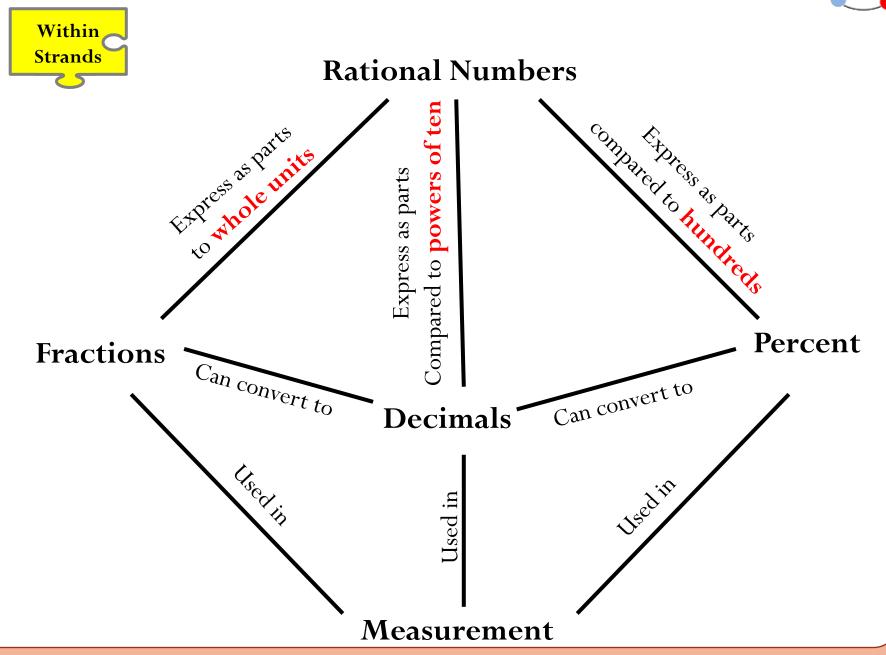
"Mathematical learning is cumulative with work at each level building on and deepening what students have learned at the previous level to foster the overall development of understanding."

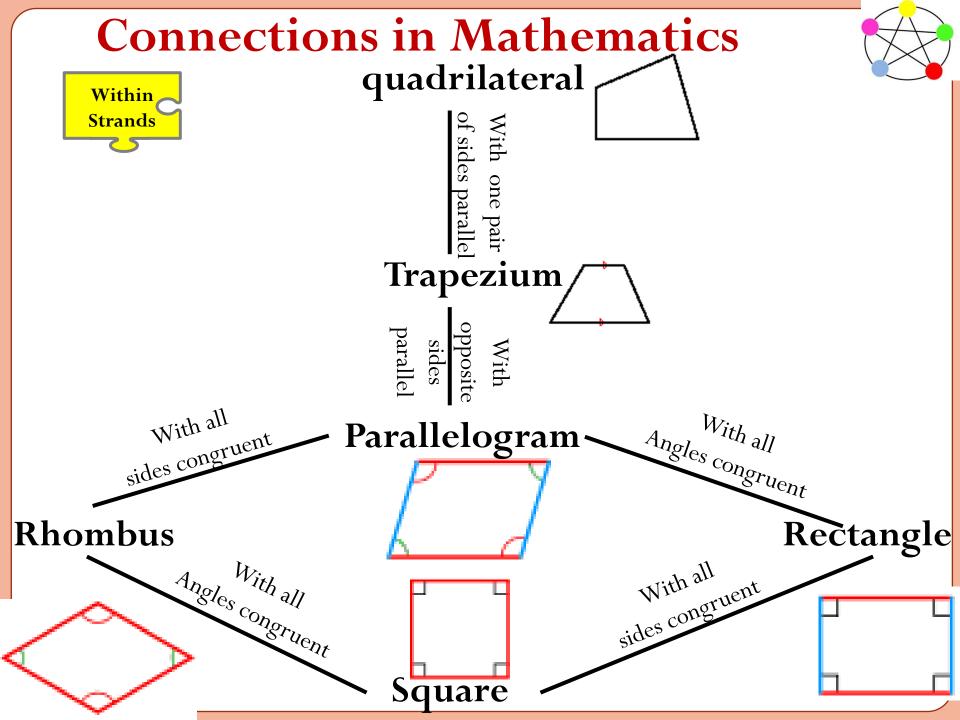
Junior Certificate Mathematics Syllabus

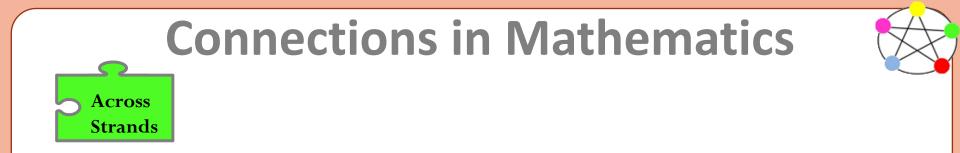




Connections that draw together key ideas and topics within a strand help students develop a more coherent understanding of the concept or process they are learning.

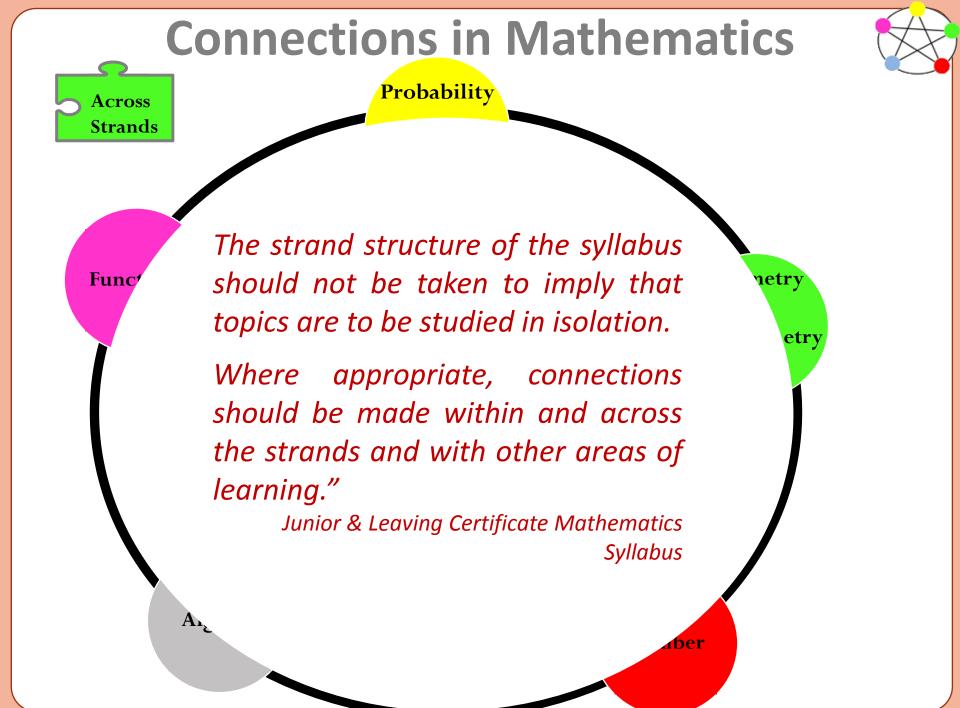


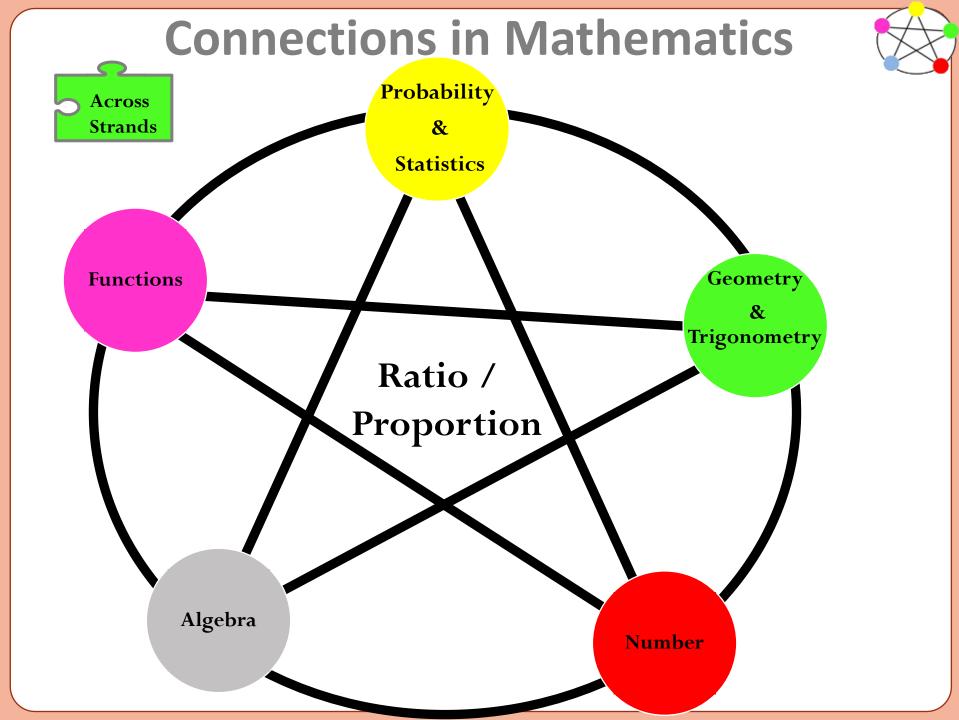




"To students, the typical curriculum presents an endless array of facts and skills that are unconnected, fragmented, and disjointed..."

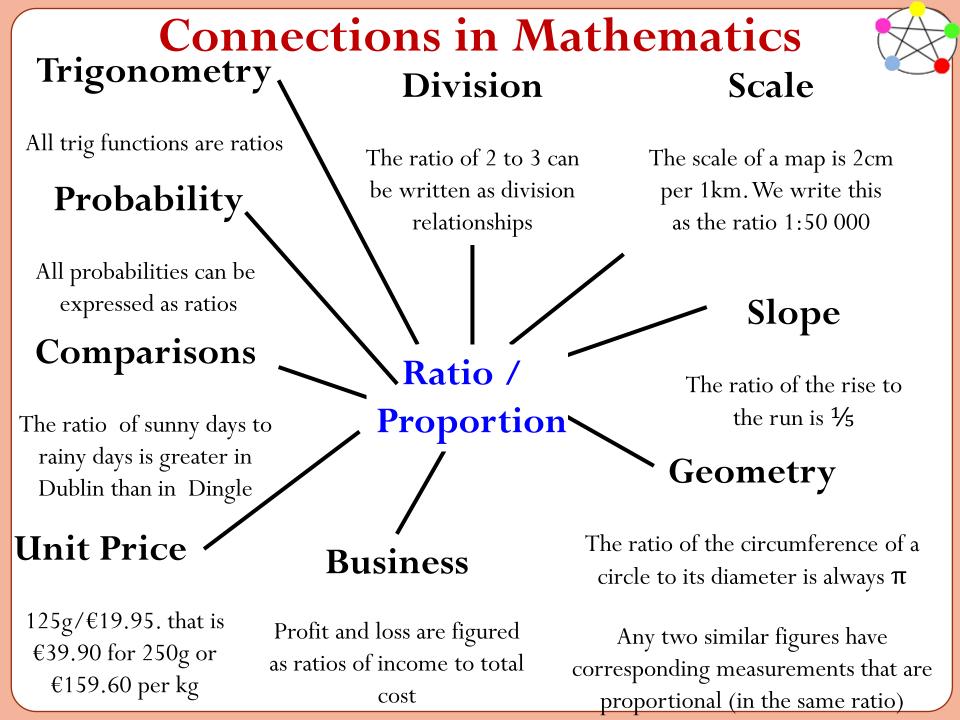
Beane, 1991

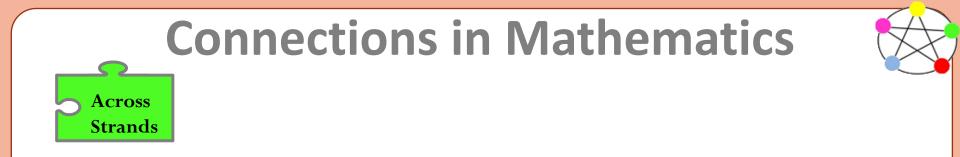




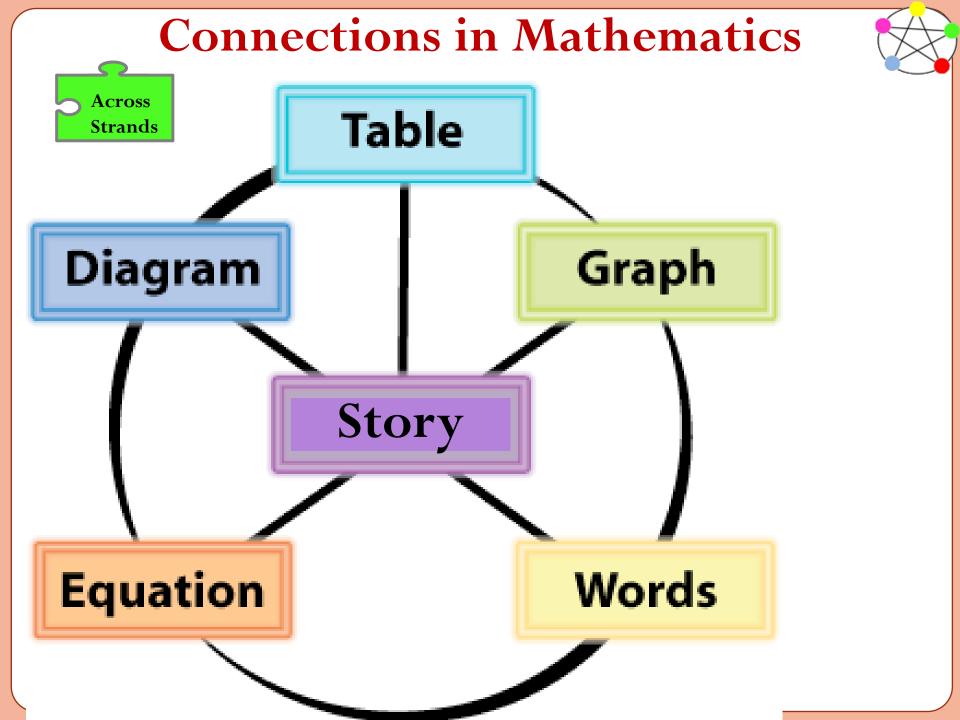


#### Ratio / Proportion



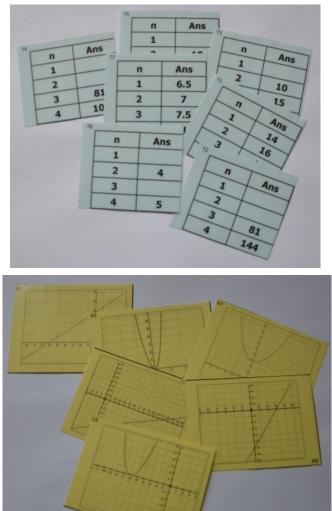


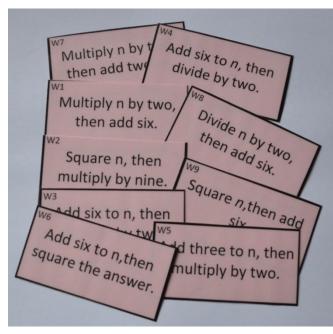
Connections to, and translations between, different representations of a concept are important cognitive processes which lead to a more robust understanding of concepts.

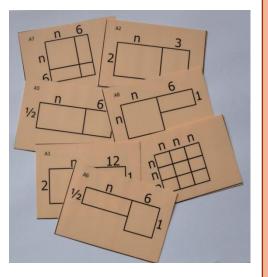


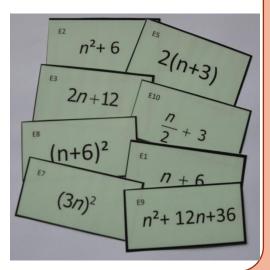














Curriculum Subjects

Mathematics is not learned in isolation. It has significant connections with other curriculum subjects.

Junior Certificate Syllabus

Science learners are expected to be able to work with data, produce graphs, and interpret patterns and trends.

In <u>**Technical Graphics**</u>, drawings are used in the analysis and solution of 2D and 3D problems through the rigorous application of geometric principles.



Curriculum Subjects

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Junior Certificate Syllabus

In <u>**Geography</u>**, learners use ratio to determine scale; graphs and statistics to analyse data</u>

In <u>Home Economics</u> learners use mathematics when budgeting and making value for money judgements



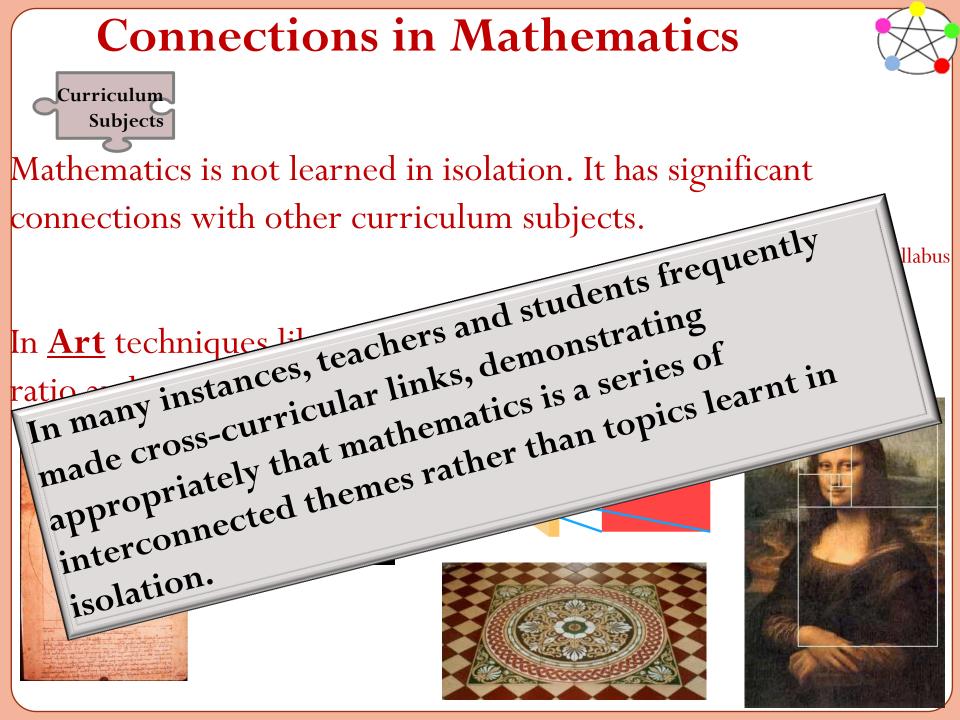
Curriculum Subjects

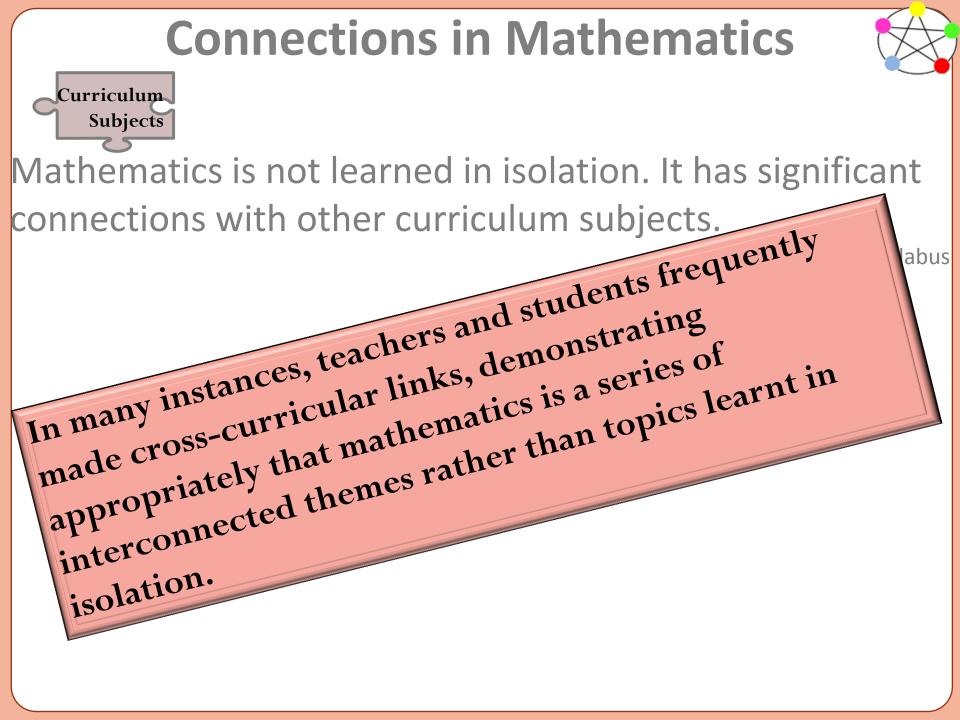
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Junior Certificate Syllabus

In <u>Business Studies</u> learners see how mathematics can be used by business organisations in budgeting, consumer education, financial services, enterprise, and reporting on accounts.

In <u>Music</u> the graph of the sound wave of a tuning fork playing a note looks like a perfect sine wave.





#### Curriculum Subjects Connections in Mathematics Accounting 2013 HL



Provide for depreciation on plant and machinery at the annual rate of 10% of cost from the date of purchase to the date of sale.

A provision for bad debts to be created equal to 4% of debtors.

The purchase price was discharged by granting the seller 380,000 shares at €1 each in Cooper Ltd at a premium of 20c per share.

On the same day goods were sold on credit to Galvin for  $\notin$ 450. This was a mark-up on cost of 25%.

Kelly borrowed €72,000 on 1/7/2012, part of which was used to purchase an adjoining warehouse costing €60,000. It was agreed that the sum borrowed would be repaid in 12 equal instalments over a six year period commencing on the 1 January 2013. Interest was to be charged at the rate of 10% per annum and paid monthly.

#### Curriculum Subjects Connections in Mathematics Accounting 2013 HL



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#### Accounting 2013 OL LC

#### Required:

(a) Prepare a statement showing Ryan's Net Worth/Capital on 01/01/2012.

(30)

Ryan also supplied the following additional information on 31/12/2012:

- During the year €14,000 was transferred from a personal bank account to the business bank account.
- (ii) During the year, Ryan had paid €6,400 out of business funds for private house repairs and had also taken goods to the value of €400 per month for private use.

Ryan estimated that on 31/12/2012 the business assets and liabilities were €960,000 and €80,000 respectively, before allowing for depreciation on furniture and equipment at the rate of 20% of cost, depreciation on motor vehicles at the rate of 10% of book value and before allowing for expenses due of €940.

(b) Prepare a statement showing Ryan's Profit or Loss for the year ended 31/12/2012. (30)

(60 marks)





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**Curriculum** Subjects **Connections in Mathematics** 

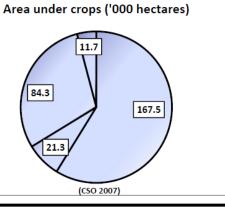


#### Agricultural Economics 2013 HL LC

In Ireland approximately 285,000 hectares of land is used for crop production. The pie chart on the right shows the number of hectares under each of the four main crop types. Complete the table below by filling in the number of hectares used for each crop type.

(one entry is completed for you)

| Сгор     | Area ('000 hectares) |
|----------|----------------------|
| Barley   |                      |
| Oats     |                      |
| Potatoes | 11.7                 |
| Wheat    |                      |



Using the above table construct a total product curve, placing the amount of fertilizer used on the horizontal x-axis and the crop yield on the vertical y-axis.

If a farm has a liquidity ratio of 0.67:1 and a net worth ratio of 0.66:1, which of the following best describes the financial position of the farm?

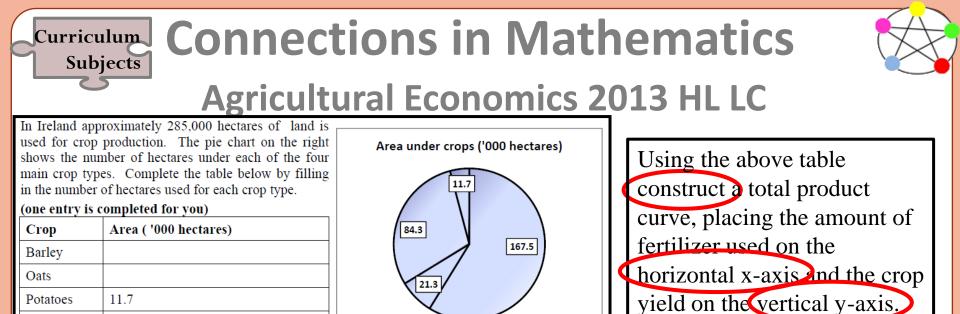
Write TRUE or FALSE after each of the following statements:

Real interest rates are nominal interest rates adjusted for inflation.

Nominal interest rates are real interest rates adjusted for inflation.

Real interest rates are negative if the inflation rate is less than nominal interest rates.

Calculate the **loan repayment capacity** of a farmer with a total annual income of  $\in 60,000$  and annual family living expenses of  $\in 40,000$  if the annual repayment on a  $\in 1,000$  loan is  $\in 250$ .



If a farm has a liquidity ratio of 0.67:1 and a net worth ratio of 0.66:1, which of the following best describes the financial position of the farm?

(CSO 2007)

Write TRUE or FALSE after each of the following statements:

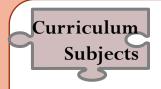
Wheat

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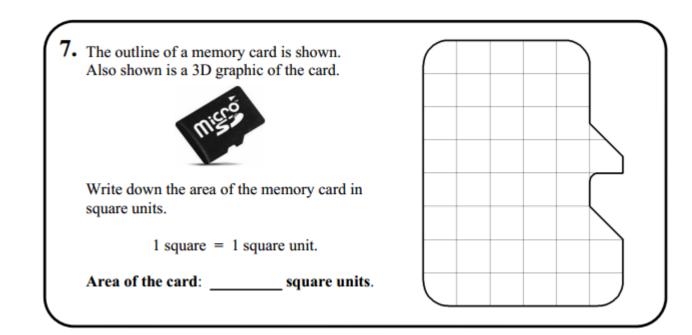
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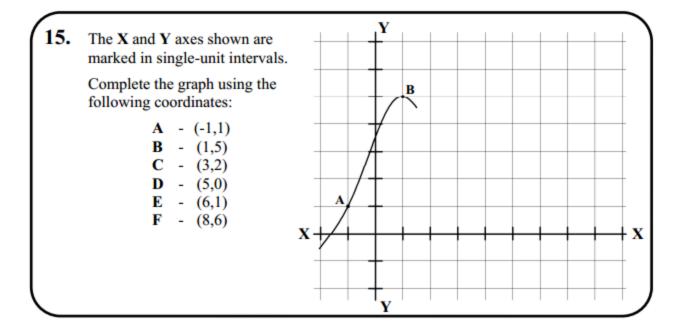
#### **Technical Graphics 2013 JC OL**







#### **Technical Graphics 2013 JC HL**

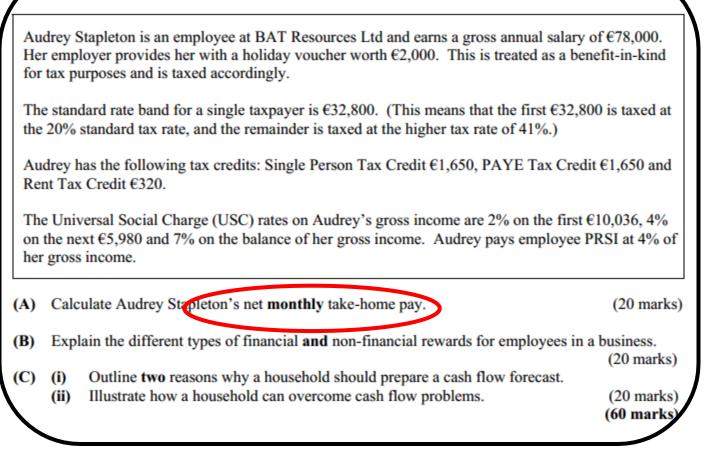






#### **Business 2013 LC HL**

#### Question 5



#### **Curriculum** Subjects **Connections in Mathematics**

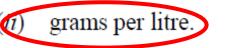


## **Chemistry 2012 HL**

Calculate, correct to two decimal places the concentration of the hydrochloric acid solution in

moles per litre,

(i)



| Loss of mass / g | 0.00 | 0.10 | 0.18 | 0.29 | 0.35 | 0.39 | 0.41 | 0.41 |
|------------------|------|------|------|------|------|------|------|------|
| Time / s         | 0    | 20   | 40   | 80   | 120  | 160  | 220  | 240  |

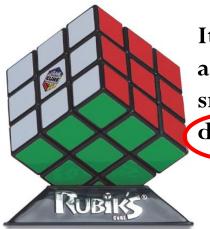
Plot a graph to show the mass of carbon dioxide produced (loss of mass) versus time. (12)

Use your graph to find the instantaneous rate of the reaction at 60 seconds in terms of g/s carbon dioxide produced. (6)

Mark clearly on your graph the curve you would expect to obtain if the reaction were repeated using 50 cm<sup>3</sup> of a 1 M solution of hydrochloric acid. Justify the shape and position of this curve relative to the graph you have plotted. (9)



## **Design & Communication Graphics 2013 HL**



It is planned to package the cube, without the stand, in a plastic sphere. Determine the diameter of the smallest possible sphere that will contain the cube and draw that sphere in the end view.

## 2012 HL

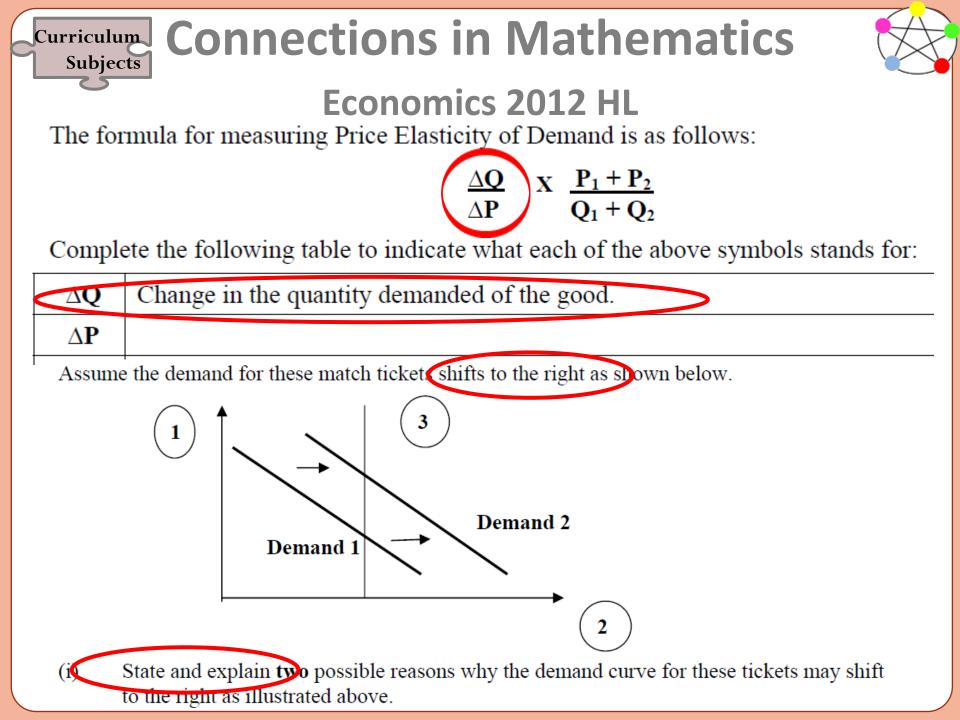
A similar cam imparts this motion to a follower:

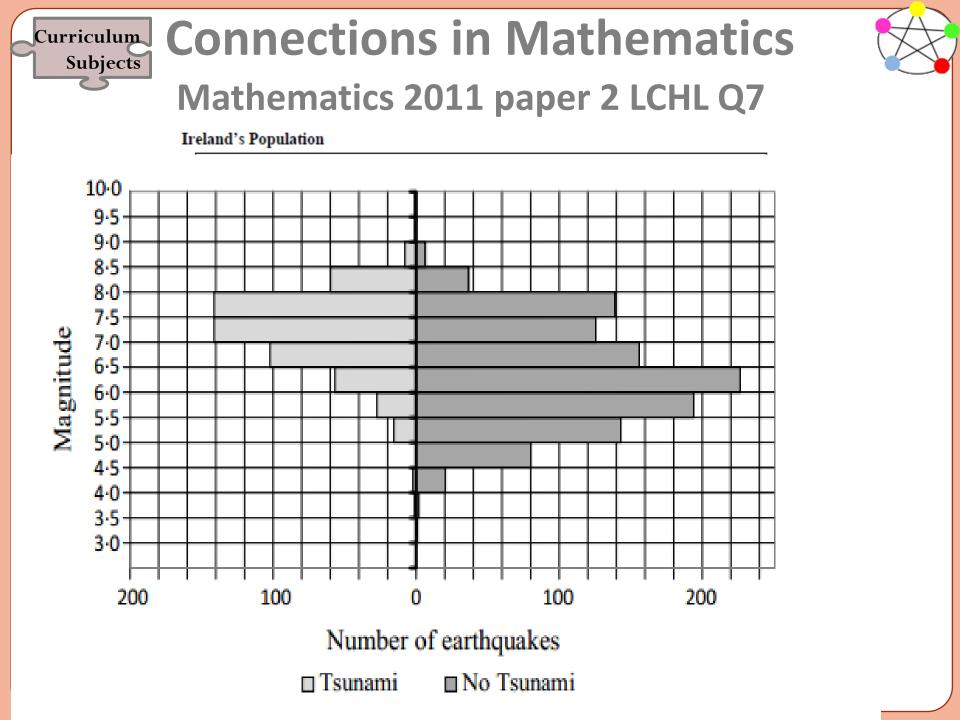
- 0° to 90° Rise 60mm with uniform velocity
- 90° to 180° Dwell
- 180° to 360° Fall 60mm with simple harmonic motion.

Draw the displacement diagram.

Note: It is not necessary to draw the profile of the cam.

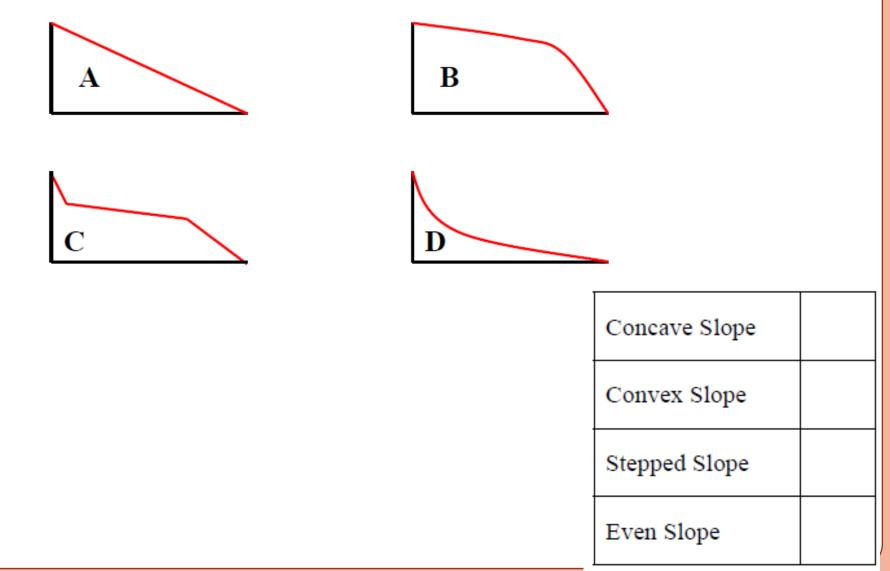
#### Scale 1:1

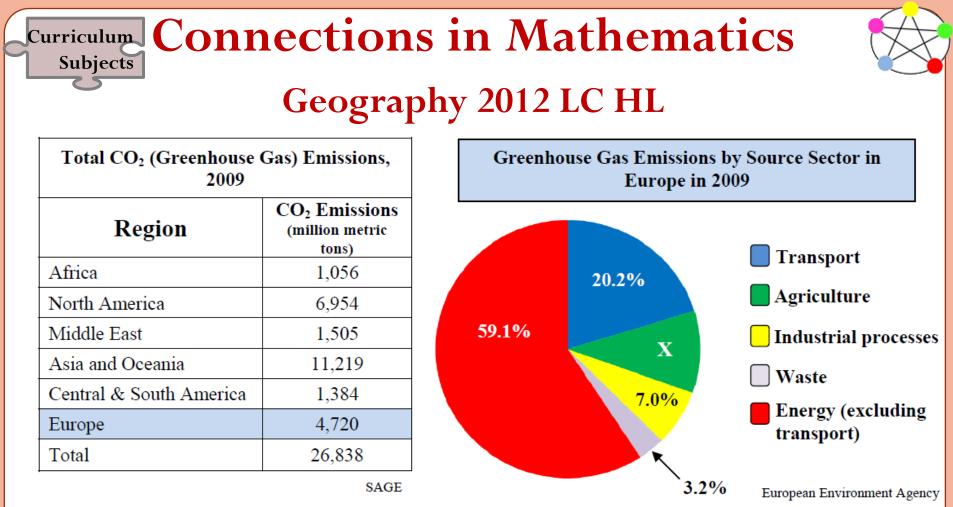




10 Slope Types

Match each of the following slope types with its correct letter in the diagram





Examine the information above and answer the following questions.

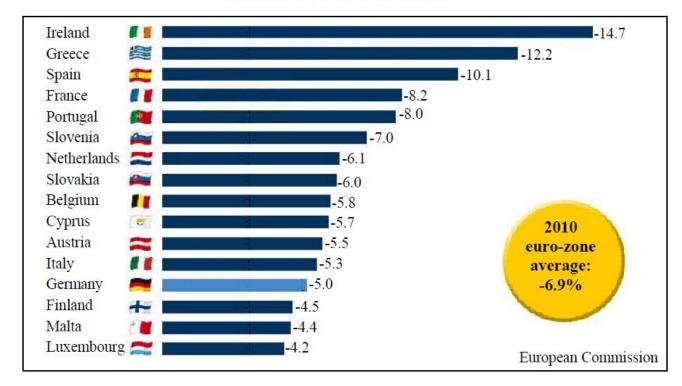
(1

Which region had the highest  $CO_2$  (greenhouse gas) emissions and which region had the lowest  $CO_2$  (greenhouse gas) emissions in 2009?

(ii) Calculate X, the percentage of greenhouse gas emissions generated by agriculture in Europe in 2009.

## Geography 2012 LC HL

Budget deficits (as a percentage of gross domestic product) of euro-zone countries in 2010



Examine the graph above and answer the following questions.

(i) How many euro-zone countries had a budget deficit greater than the euro-zone average in 2010?
(ii) What was the difference in the budget deficit (as a percentage of gross domestic product) between freland and Austria in 2010?

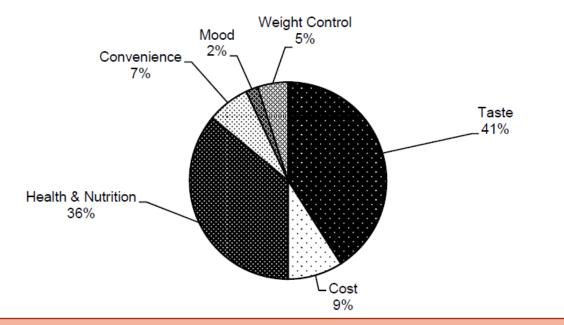


### Home Economics Scientific & Social 2012 HL

|                                  | 2006 | 2007 | 2008              | 2009  | 2010  | 2011  |
|----------------------------------|------|------|-------------------|-------|-------|-------|
| Unemployment<br>rates in Ireland | 4.4% | 4.5% | <mark>6.4%</mark> | 11.8% | 13.7% | 14.2% |

(Seasonally adjusted standardised unemployment rates. Central Statistics Office)

(i) Having regard to the information provided above, discuss unemployment in Ireland.



## Physics 2012 HL

In an experiment to investigate the variation of the fundamental frequency f of a stretched string with its length l, the following data were recorded.

| <i>f</i> /Hz | 95    | 102   | 114   | 126   | 141   | 165   | 194   | 232   |
|--------------|-------|-------|-------|-------|-------|-------|-------|-------|
| l/m          | 0.603 | 0.553 | 0.503 | 0.453 | 0.403 | 0.353 | 0.303 | 0.253 |

Using the data, draw a suitable graph on graph paper to show the relationship between the fundamental frequency of the stretched string and its length.

Cork and Sligo are about 330 km apart by road. Using the map of Ireland shown on page 4, estimate the displacement of Sligo from Cork. The scale of the map is 1 cm to 37.5 km.

The European aerospace group EADS is developing a hypersonic jet aircraft that will fly at four times the speed of sound, 330 m s<sup>-1</sup>. Express the speed of the aircraft in kilometre per hour.

(radius of earth  $\neq 6.36 \times 10^6$  m; mass of earth  $= 5.97 \times 10^{24}$  kg)

Explain the shape of your graph.

#### Curriculum Subjects Connections in Mathematics



## Physics 2012 OL

The following table shows the values recorded for the current I and the corresponding potential difference V during the experiment.

| V/V | 0 | 1.0 | 2.0 | 3.0 | 4.0 | 5.0 | 6.0 |
|-----|---|-----|-----|-----|-----|-----|-----|
| I/A | 0 | 0.4 | 0.8 | 1.2 | 1.6 | 2.0 | 2.4 |

Using the data in the table, draw a graph on graph paper to show the variation of current with potential difference.

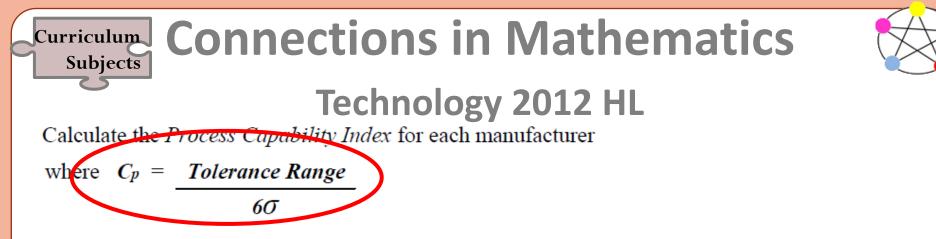
Calculate the slope of your graph.

A plug is used to connect an electrical appliance in the home to the 230 volt mains supply. Modern plugs contain a small fuse which comes with a rating of 1A, 2A, 3A, 5A or 13A. The electrical energy supplied to the home is measured in kW h (*kilowatt-hour*).

If the vacuum eleaner is used for 90 minutes, calculate

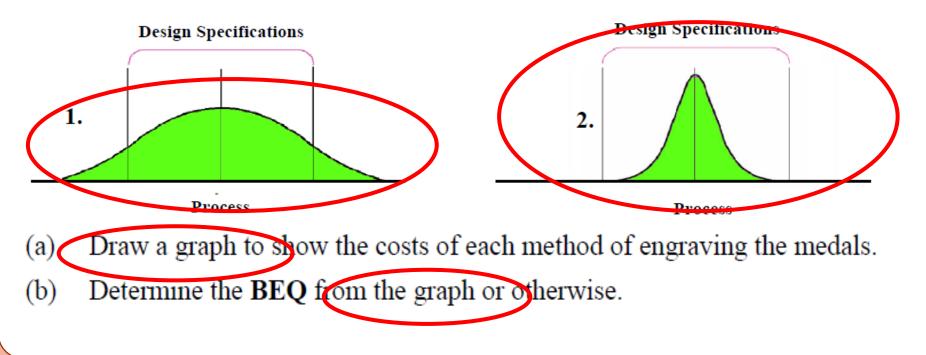
(vii) the number of units of electricity used;

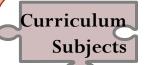
(viii) the cost of the energy used if the price of each unit of electricity is 22 cent.



Which manufacturer should be chosen so that the bearings will always meet design specifications? Give **one** reason for your answer.

Identify the graph which best represents the Process Capability of each manufacturer.







## Technology 2013 HL

| Day            | July 11 <sup>th</sup> | July 12 <sup>th</sup> | July 13 <sup>th</sup> | July 14 <sup>th</sup> | July 15 <sup>th</sup> | July 18 <sup>th</sup> | July 19 <sup>th</sup> |
|----------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| No. of defects | 10                    | 8                     | 11                    | 10                    | 9                     | 10                    | 12                    |



- The mean of the process
  The UCL
  The LCL.
- (ii) Draw a suitable control chart for the above data.
- (iii) Interpret the control chart drawn at (ii) above and comment on the control state of the process.

## Curriculum Subjects Connections in Mathematics



# Chemistry 2013 LC HL

 (a) The 350<sup>th</sup> anniversary of Robert Boyle's discovery of the relationship between the pressure and the volume of a fixed mass of gas at constant temperature is commemorated in this Irish stamp issued in 2012.

Boyle also contributed to the development of the use of the term *element* in Chemistry.

What was his understanding of this term?



(b) Use Bohr's atomic theory of 1913 to account for the emission spectrum of the hydrogen atom. (15) Explain, in terms of atomic structure, why different flame colours are observed in flame tests using salts of different metals. (6)

(5)

What colour is observed in a flame test on lithium chloride?

Describe the testing procedure.

(c) Further research and scientific discoveries, including Heisenberg's <u>uncertainty principle</u> (1927), led to significant modification of Bohr's original atomic structure theory of 1913. Explain the underlined term.

Give one other factor that also contributed to the need for modification of Bohr's 1913 theory.

These modifications included the introduction of the idea of atomic orbitals.

What is an atomic orbital?

(15)

(9)

#### **Connections in Mathematics** Curriculum Subjects Numeracy encompasses the ability to use mathematical understanding and skills to solve problems and meet the demo Discussion at department meetings should take place of a to identify and develop agreed approaches to the e Lite teaching of common procedures in Mathematics. situations ppned to solve problems. addes the capacity to read, understand and critically appreciate various forms of communication including spoken language, printed text, broadcast media, and digital media.

LITERACY AND NUMERACY FOR LEARNING AND LIFE The National Strategy to Improve Literacy and Numeracy among Children and Young People 2011-2020

Curriculum

Subjects



Numeracy encompasses the ability to use mathematical understanding and skills to solve problems and meet the demands of day-to-day living in complex social settings. To have this ability, a young person needs to be able to think and communicate quantitatively, to make sense of data, to have a spatial awareness, to understand patterns and sequences, and to recognise situations where mathematical reasoning can be applied to solve problems.

Literacy includes the capacity to read, understand and critically appreciate various forms of communication including spoken language, printed text, broadcast media, and digital media.

LITERACY AND NUMERACY FOR LEARNING AND LIFE The National Strategy to Improve Literacy and Numeracy among Children and Young People 2011-2020

Curriculum

Subjects



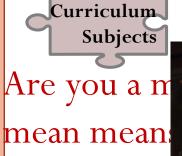
# **Vocabulary Difficulties**

Are you a mean teacher if you do not tell your students what the mean means?

I am right when I say, in your right hand you are holding a right angle

On foot of measuring the man's foot I know that it is a foot long.

**Vocabulary Difficulties** 



I am right w angle

On foot of 1



ing a right

a foot long.

# IT SAID PUT IT INTHE **OVEN AT 130 DEGREES**



# **Vocabulary Difficulties**

Curriculum

Subjects

| Category of difficulty  | Examples   |
|---|--|
| Some words are shared by  | Right angle versus right answer  |
| mathematics and everyday English,                               | Right angle versus right hand  |
| but have different meanings in the                              | Reflection as flipping over a line versus reflection as  |
| two contexts  | thinking about something   |
|   | Foot as twelve inches versus the foot of a leg   |
| with English and have comparable                                | Difference as the answer to subtraction versus<br>difference as a general comparison<br>Even as divisible by two versus even as smooth |
| meaning is more precise   |  |
| Some mathematical terms are found only in mathematical contexts | Quotient, decimal, denominator, quadrilateral, parallelogram,isoceles  |

Curriculum

Subjects



# **Vocabulary Difficulties**

| Category of difficulty        | Examples   |
|-------------------------------|--|
| Some words have more than one | Round as a circle versus to round an answer              |
| mathematical meaning          | Square as a shape versus square as a number times itself |
|                               | Second as a measure of time versus second as a location  |
|                               | in a set of ordered items                                |
|                               | Side of a rectangle as a line segment versus side of a   |
|                               | prism as a rectangle                                     |

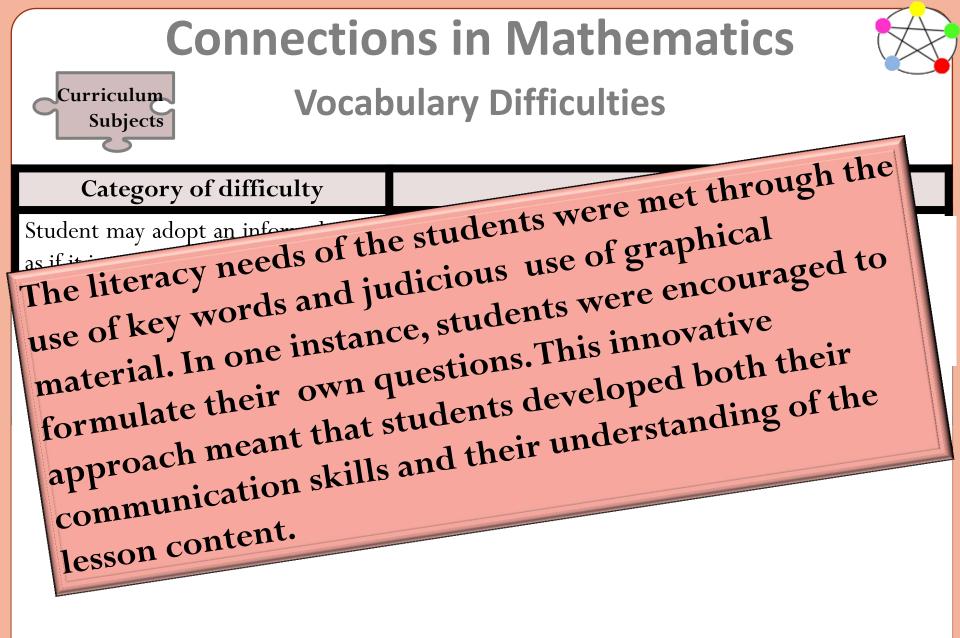
Curriculum

Subjects



## **Vocabulary Difficulties**

| Category of difficulty           | Examples   |
|----------------------------------|--|
| Some mathematical terms are      | Sum versus some  |
| homonyms with everyday English   | Arc versus ark   |
| words                            | Pi versus pie  |
|                                  | Graphed versus graft                                   |
| Some mathematical words are      | Factor and multiple, hundreds and hundredths,          |
| related but students may confuse | numerator and denominator                              |
| their distinct meanings          |  |
| Some mathematical concepts are   | Skip count by threes versus say the multiples of three |
| verbalised in more than one way  | One quarter versus one fourth                          |
|                                  | Cubed root versus third root                           |
|                                  | Squared versus power of two                            |



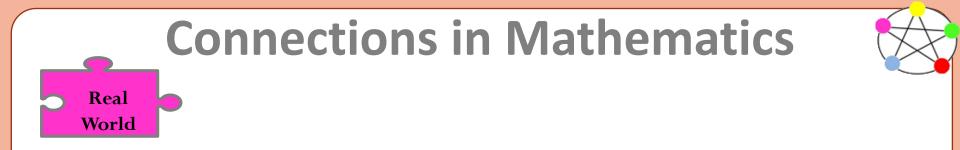


## **Vocabulary Difficulties**

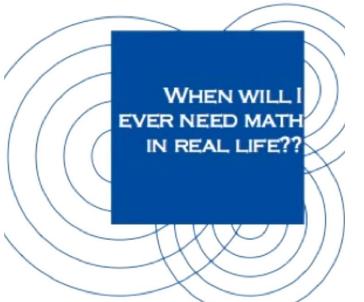
Curriculum

Subjects

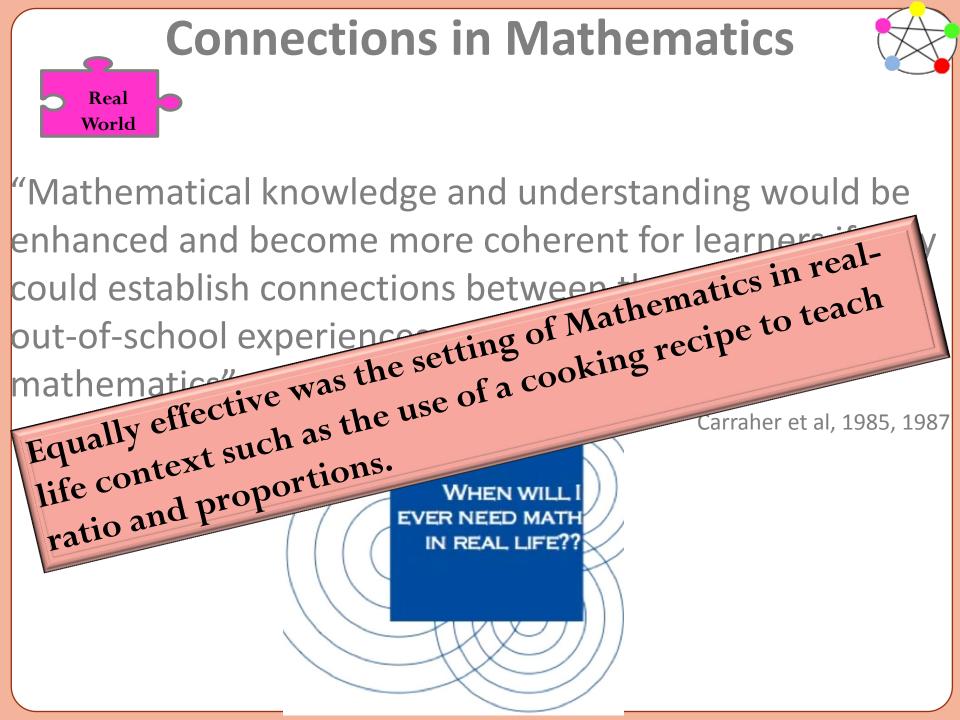
| Category of difficulty              | Examples  |
|-------------------------------------|---|
| Student may adopt an informal term  | Diamond for rhombus                                       |
| as if it is a mathematical term     | Corner for vertex   |
| English spelling and usage has many | Four has a u but forty does not                           |
| irregularities                      | Fraction denominators such as sixth, fifth, fourth, third |
|                                     | are like ordinal numbers but rather than second the       |
|                                     | next fraction is half                                     |



"Mathematical knowledge and understanding would be enhanced and become more coherent for learners if they could establish connections between the 'networks' of out-of-school experiences and those of in-school mathematics"



Carraher et al, 1985, 1987



## Connections in Mathematics Real World

"In each strand, and at each syllabus level, emphasis should be placed on making connections between the strands and on appropriate contexts and applications of mathematics so that learners can appreciate its relevance to current and future life."

Junior Certificate Syllabus

### Review



Identified the importance for Teaching & Learning of making connections

Considered the types of connections it is beneficial to make

Alerted ourselves as educators to the importance of connecting with the school literacy and numeracy policy.

