## Exploring the relationship between the Argument and Modulus when multiplying complex numbers

Follow this link to answer the questions below: https://www.geogebra.org/classic/bmedez74
How do we find the Argument of a complex number?


What do you notice about the Arguments when 2 complex numbers are multiplied?


How do we find the modulus of a complex number?


What do you notice about the moduli when 2 complex numbers are multiplied?


What do you think would happen if we were to multiply a complex number by itself?

What would happen if we were to cube that complex number?

Can you see a pattern? (click on the button to reveal exponents of $z$ )


The effect of multiplying a complex number by itself (complete the table):

| Multiplication of a <br> complex number | Argument (angle $\boldsymbol{\theta}$ ) | Modulus ( $r$ ) |
| :--- | :--- | :--- |
| $\mathbf{z x z = z ^ { 2 }}$ | Double the argument (20) | Square the modulus ( $\left.\mathbf{r}^{\mathbf{2}}\right)$ |
| $\mathbf{z x z x z =}$ |  |  |
|  |  |  |
|  |  |  |
| z |  |  |

The effect of multiplying a complex number by itself:

| Multiplication | Argument (angle $\theta$ ) | Modulus (r) |
| :---: | :---: | :---: |
| $\mathrm{zx} \mathrm{z}=\mathrm{z}^{2}$ | Doubled (20) | Squared ( $\mathrm{r}^{2}$ ) |
| $z \mathrm{xzxz}=\mathrm{z}^{\mathbf{3}}$ | Tripled (30) | Cubed ( $\mathrm{r}^{3}$ ) |
| zxzxzxz= $z^{4}$ | Multiplied by 4 (40) | Multiplied by itself 4 times ( $\mathrm{r}^{4}$ ) |
| zxzxzxzxz= ${ }^{5}$ | Multiplied by 5 (50) | Multiplied by itself 5 times ( $\mathrm{r}^{5}$ ) |
| $z^{\text {n }}$ | Multiplied by $\mathrm{n}(\mathrm{n} \theta$ ) | Multiplied by itself n times ( $\mathrm{r}^{\mathrm{r}}$ ) |

De Moivre's theorem: $z^{n}=r^{n}(\cos n \theta+i \sin n \theta)$

